Introduction

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What is statistics?

- Statistics is the science of learning from experience
- In principle, people do this every day of their lives, and should be really good at it . . .
- . . .but we’re not.
Limitations of human reasoning

- Human beings are not natural statisticians
- We are not good at picking out patterns from a sea of noisy data
- On the flip side, we are *too good* at picking out non-existent patterns from small numbers of observations
- We also find it difficult to sort out the effects of multiple factors occurring simultaneously
- Finally, we are subject to all sorts of biases depending on our personalities, emotions, and past experiences
In medicine, public health, and the biological sciences, we must often make decisions in the presence of uncertainty:

- Which drug should a doctor prescribe to treat an illness?
- An individual has a certain genetic mutation; what are the chances that she will develop breast cancer?
- Does a certain pesticide cause cancer? Should it be banned?

These questions are too important to be left to opinion, superstition, and conjecture, which is why there has been a tremendous push for objective, evidence-based decision making in medicine and public health in the past several decades.
Statistics is the science which allows us to make these decisions

Statistics is particularly important in research concerning humans, for several reasons:

- Humans are incredibly diverse and variable
- Humans are expensive to perform research upon
- There is a moral imperative to make decisions on potentially life-saving therapies as fast as possible

For these reasons, Biostatistics has emerged as an important field within statistics, and has become an important set of skills in fields such as medicine, biology, and public health
Scientists want to make generalizations about classes of people on the basis of their findings.

The class of people that they are trying to make generalizations about is called the population.

It is impractical to study the entire population, so people study only a small portion of it called the sample.

The researchers then make generalizations about the entire population based on studying the sample; this process is called inference.
Population

Sample

Study design

Inference

Population

Study
design

Inference

Sample
The three basic questions in statistics

• How should I collect my data?
• How should I describe and summarize the data that I’ve collected?
• What does my data tell me about the way that the world works (inference)?
Specifically, there is some numerical fact about the population that the investigator is interested in, such as the percent of children who are obese or the average reduction in cholesterol upon taking a certain drug.

These numbers that describe the population are called parameters.

Parameters cannot be observed directly; they can only be estimated from a sample.

An estimate (or statistic) is a number that can be computed from a sample.
How good are our estimates?

So,
- Estimates are what investigators know
- Parameters are what investigators want to know

We would like to know whether or not our estimate is measuring the parameter of interest well

There are two major issues:
- On average, does our estimate tend to be centered around the right answer, or is it biased?
- How much variability is there likely to be in our estimate?
We’ve discussed three important pairs of concepts:
- Population / Sample
- Parameter / Estimate
- Bias / Variability

The conceptual framework of statistics is represented in this figure (slide 7):